High-Pressure Vapor–Liquid Equilibria, Liquid Densities, and Excess Molar Volumes for the Carbon Dioxide + 2-Propanol System from (308.10 to 348.00) K

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Vapor—liquid equilibrium data and volumetric properties (density and excess molar volumes) of the carbon dioxide (1) + 2-propanol (2) system have been determined for seven molar compositions, z_1 , close to 0.15, 0.20, 0.42, 0.60, 0.80, 0.95, and 0.97, using a vibrating tube densimeter, which takes advantage of a forced path mechanical calibration model. The Peng–Robinson equation of state including Panagiotopoulos and Reid mixing rules is used to correlate the data. Comparison of the new data with selected literature data and correlated results shows good consistency agreement, demonstrating the reliability of the data presented herein.

1. Introduction

Supercritical fluid extraction (SFE) is a more and more used technology. It is receiving increasing attention from both industry and academic researchers. The basic steps of a SFE process are the following:

(1) The material (solid or liquid) containing the compound to be extracted is put in contact with a high-pressure supercritical fluid (SF) (pure or mixed with a cosolvent for selectivity purposes),¹ and the compound is partially dissolved selectively into the supercritical phase.

(2) The compound can be recovered by a pressure or temperature change of the system. SFE has several advantages as many substances are more soluble in high-pressure supercritical fluids than in liquids at ambient conditions. As diffusion coefficients are higher in supercritical fluids than in liquids, mass transfers are consequently faster. The viscosity of SF is much lower than that of liquids, which is also clearly advantageous.

The most common compound used as a SF in SFE is carbon dioxide: CO_2 is a very attractive compound because it is cheap, nontoxic, and its critical temperature (304.21 K) is close to the ambient temperature, which allows smaller heating-cooling costs. CO_2 at high pressure is also a good sterilizer for food products. Industry needs very accurate thermodynamic models for designing and optimizing SFE separation processes. Among the important properties used in SFE are the volumetric properties.

 CO_2 cannot be universally used, as it is a nonpolar compound. Then, it has no strong interaction with polar components and consequently no favored selectivity. To solve this problem, cosolvents are generally added to CO_2 . Cosolvents change the SF fluid density and critical properties. In addition, they can produce strong interactions with solutes, i.e., hydrogen bonds, dipole interactions, etc. In this paper, the studied cosolvent is isopropanol. It is a polar compound able to create H bonds with solutes to be extracted selectively.

The use of cosolvents (such as alcohols) in combination with one supercritical solvent (e.g., carbon dioxide) has motivated new phase equilibrium measurements. Process design and

* Corresponding author. E-mail: dominique.richon@ensmp.fr. Telephone: (33) 164694965. Fax: (33) 164694968. optimization of operating conditions relies strongly on accurate thermodynamic data in large temperature and pressure ranges. In this paper, we have considered 2-propanol as the cosolvent to CO₂. Limited information is available about vapor—liquid equilibrium data, and even less is available about $P\rho T$ properties in the liquid phase for the carbon dioxide (1) + 2-propanol (2) binary system as indicated in refs 2 and 3.

A "synthetic open circuit method" taking advantage of a vibrating tube densimeter is used to determine, at and outside saturation conditions, volumetric properties in isothermal conditions of either pure compounds or mixtures in vapor, liquid, and supercritical conditions. The Peng–Robinson equation of state⁴ (PR EoS) is used to correlate the data at saturation.

2. Experimental Section

Apparatus. A detailed description of the typical apparatus is available elsewhere (Bouchot and Richon⁵). Its flow diagram is presented in Figure 1. The apparatus used in this work utilizes an Anton Paar DMA 512P vibrating tube (Figure 1). The vibrating tube is made of Hastelloy and can work up to 70 MPa. It has already provided data for the ethane and hydrogen sulfide binary mixture.⁶ The period of the vibration, τ , in seconds, is recorded with a HP53131A data acquisition unit (12). The uncertainty of vibrating period values is $\pm 10^{-8}$ s. The temperature of the vibrating tube is controlled by a regulated liquid bath (LAUDA RE206) with stability within \pm 0.01 K. The temperature of the remaining parts of the circuit is regulated by a (HUBER Variostat P1C50P) liquid bath. Temperatures are measured by two Pt100 probes (11 and 14) connected to the HP34970A data acquisition unit (13). These Pt100 probes are periodically calibrated against a 25 Ω reference thermometer (TINSLEY Precision Instrument) certified by the Laboratoire National d'Essais (Paris, France). Resulting uncertainties in temperatures are within ± 0.01 K. A vacuum was achieved by means of a vacuum pump (AEG type LN38066008). Pressures are measured using three pressure transducers (Druck PTX611) of three complementary ranges: (0 to 0.2) MPa, (0 to 5) MPa, and (0 to 40) MPa. These sensors were calibrated against a dead weight pressure balance (Desgranges & Huot model 5202S) for the (0.3 to 40) MPa pressure range and against an electronic balance (fundamental digital pressure standard, Desgranges & Huot model 24610, France) for pressures below 0.3 MPa. The



Figure 1. Flow diagram of the equipment: 1, loading cell; 2a and 2b, regulating and shut-off valves; 3, DMA 512 P densimeter (Anton Paar); 4, heat exchanger; 5, bursting disk; 6, inlet of the temperature regulating fluid; 7a and 7b, regulating and shut-off valves; 8, pressure sensors maintained at constant temperature (373.15 K); 9, vacuum pump; 10, vent; 11, vibrating cell temperature sensor; 12, HP 53131A unit; 13, HP34970A unit; 14, bath temperature sensor; 15, liquid bath.

Table 1. Pure Compound Properties (from Ref 12)

			М	$P_{\rm C}$	T _C	$v_{\rm C} \cdot 10^{-5}$	$\rho_{\rm C}$
compd	formula	CAS No.	kg•mol ⁻¹	MPa	K	$\overline{m^3 \cdot mol^{-1}}$	kg•m ⁻³
carbon dioxide	CO ₂	124-38-9	0.04401	7.374	304.12	9.4	468.2
2-propanol	C_3H_8O	67-63-0	0.0601	4.762	508.3	22	273.2

pressure transducers are connected to the HP34970A data acquisition unit. Real time data are recorded every 3 s by a computer linked to both HP units. Knowledge of the composition of the mixtures prepared inside the loading cell (1) is deduced from its double weighing before and after introducing each component through a previously evacuated line. A CC3000 analytical balance, from Sartorius AG Göttingen, was used to get accurate mass values. Uncertainties of mass determinations are $\pm 10^{-4}$ g.

Materials. Carbon dioxide is from Air Liquide with a certified purity higher than 99.99 % volume fraction. 2-Propanol is from Prolabo with a certified purity higher than 99 % volume fraction (see Table 1).

Experimental Procedure. First, the baths are programmed at constant temperatures with a small temperature difference corresponding to the requested measurements: bubble or dew pressures (see ref 5 for details). The whole circuit was evacuated using the vacuum pump (with the 9, 7a, and 7b valves open while valves 10 and 2b are closed). During this time, the mixture was prepared into the loading cell (1) according to the method described by Bouchot and Richon⁵ and Galicia-Luna et al.⁷ A few period values are recorded to have a reference vibrating period at the lowest accessible pressure ($< 5 \cdot 10^{-4}$ MPa) with classical vacuum pumps. After connecting the loading cell to the circuit through valve 1b, a vacuum is achieved up to 1b by opening valves 2a and 2b. The loading cell is also connected to a high-pressure cylinder to pressurize the mixture to a pressure much higher than its bubble point pressure, maintaining it in the homogeneous liquid state even when loading the vibrating tube. Then, valves 7a and 2b are closed and valve 1b is opened.

Small amounts of fluid (small flow rates controlled by regulating valve 2b) can be continuously introduced into the vibrating tube. Then, the pressure increases continuously up to the dew point at a controlled rate with a maximum of 0.005 MPa·s⁻¹. During this process, the fluid is assumed to be in equilibrium, and pressure, period, and temperature $(P\tau T)$ are recorded every 2 s. After recording the dew point (determined through the drastic slope change observed in the $P\tau$ or $P\rho$ curves) behavior going from single phase to diphasic properties (as described by Bouchot and Richon⁵), the fluid is fully condensed in the whole circuit by increasing pressure up to the chosen maximum pressure of the study (approximately from (10 to 15) MPa in this work). Valves 9 and 10 were closed, and valve 7a was opened. The condensation over a pressure range leads to a composition gradient inside the vibrating tube and circuit. It should be noted that it is necessary to introduce a fresh mixture from the loading cell to purge the circuit. By opening valve 10, the fluid was allowed to circulate (it is assumed that the liquid inside the vibrating tube is representative of the fluid from the loading cell when the measured period remains constant and is not dependent on further purging). The liquid phase is studied from the chosen upper pressure limit down to the bubble point determined through the drastic change in the $P\tau$ (or $P\rho$) behaviors going from single phase to diphasic properties as described by Bouchot and Richon.⁵ The pressure decreases continuously at a controlled rate of a maximum of 0.005 MPa·s⁻¹ using regulating valve 7a. During this process, the fluid is assumed to be in equilibrium, and pressure, period (τ), and temperature ($P\tau T$) are recorded every 2 s. Periods are converted into density values using the forced path mechanical calibration model (FPMC, Bouchot and Richon⁸), whose parameters were calculated from (PFT) data of a reference fluid (R134a), whose thermodynamic properties are well described by Tillner-Roth and Baehr.9

Estimation of Uncertainties (Taking into Account Expanded Uncertainties and Coverage Factors as Described in http:// physics.nist.gov/cuu/Uncertainty/index.html). The global un-

Table 2. Liquid Densities and H	Excess Molar	Volumes of the C	arbon Dioxide	(1) + 2-Propanol (2) Binary	System for	Seven Mole	Fractions and
Five Temperatures at Various F	Pressures							

Р	ρ	$v^{\rm E}$	Р	ρ	$v^{\rm E}$	Р	ρ	$v^{\rm E}$
MPa	kg•m ⁻³	$\overline{\text{cm}^3 \cdot \text{mol}^{-1}}$	MPa	kg•m ⁻³	$\overline{\text{cm}^3 \cdot \text{mol}^{-1}}$	MPa	kg·m ⁻³	$\overline{\text{cm}^3 \cdot \text{mol}^{-1}}$
ر	$x_1 = 0.139_6; T/K = 3$	308.11	<i>x</i> ₁	$= 0.139_{6}; T/K =$	313.09	<i>x</i> ₁ =	$= 0.139_{6}; T/K =$	323.05
1.814	786.2	-173.5	2.502	781.7	-122.1	2.995	771.3	-103.2
2.252	786.8	-135.1	3.002	782.3	-97.8	3.503	771.9	-84.9
3.003	787.7	-95.2	3.513	782.9	-80.0	4.003	772.6	-/1.4
3.200	788.2	-80.2	4.008	783.5	-56.8	4.494 5.074	773.9	-51.3
3.607	788.4	-74.9	5.001	784.7	-48.5	5.511	774.5	-45.3
4.089	788.9	-62.9	5.497	785.3	-41.5	6.033	775.2	-39.2
5.013	789.9	-46.1	6.023	785.9	-35.3	7.021	776.4	-29.9
5.503	790.5	-39.3	6.504	786.5	-30.3	7.514	777.1	-26.1
6.019	791.0	-33.0	7.026	787.1	-25.5	8.002	779.2	-22.7
7.009	791.7	-27.7 -22.8	7.469	788.2	-21.3 -17.2	0. <i>321</i> 9.033	778.8	-19.4 -16.5
7.512	792.7	-17.6	8.509	788.8	-12.9	9.519	779.4	-14.0
8.016	793.3	-10.5	8.995	789.3	-9.4			
8.530	793.9	-7.2	9.503	789.8	-7.6			
8.990	794.3	-6.3						
9.498	794.8	-5.7						
ŗ	$x_1 = 0.139_6; T/K = 3$	332.99	x_1	$= 0.139_6; T/K =$	347.95	$x_1 =$	$= 0.2003_4; T/K =$	308.11
2.861	759.8	-114.1	3.317	742.5	-102.2	3.514	792.7	-110.5
3.000	760.0	-107.9	3.516	742.7	-95.3	4.006	793.4	-92.1
3.297	760.4	-96.3	4.002	743.5	-81.4 -71.0	4.510	794.0	-//.2
4 008	761.5	-89.0 -75.4	5.008	744.3	-61.2	5 504	794.7	-55.2
4.509	762.2	-64.6	5.502	745.9	-53.9	6.006	795.9	-46.4
5.030	762.8	-55.7	6.011	746.7	-47.7	6.517	796.5	-38.5
6.502	764.9	-38.0	6.501	747.5	-42.6	7.029	797.2	-31.1
7.005	765.6	-33.6	7.037	748.3	-37.9	7.516	797.7	-23.9
7.501	766.3	-29.8 -26.4	7.523	749.1	-34.2 -30.8	8.001	798.3	-14.1
8 521	767.6	-23.4	8 497	749.8	-28.0	9.019	798.9	-7.6
9.040	768.3	-20.6	8.993	751.3	-25.4	10.003	800.7	-6.3
9.511	768.8	-18.4	9.568	752.1	-22.7	10.047	800.8	-6.3
9.974	769.5	-16.4	10.032	752.8	-20.8			
x	$T_1 = 0.2003_4$; $T/K =$	313.10	<i>x</i> ₁ =	$= 0.2003_4$: T/K =	323.07	$x_1 =$	$= 0.2003_4$; T/K =	333.05
3.601	786.8	-110.3	4.004	775.4	-101.5	4.210	763.4	-100.6
4.007	787.4	-95.3	4.307	775.8	-91.9	4.492	763.8	-92.2
4.523	788.1	-79.9	4.497	776.1	-86.5	4.799	764.3	-84.2
5.069	/88./ 780.3	-67.0	4.802	//0.0 776.0	-/8.8	5.001	/64.6 765.3	-/9.4 -69.8
6.027	789.3	-38.3 -49.4	5.510	777.5	-63.9	5 996	765.3	-60.7
6.504	790.7	-42.3	6.029	778.3	-55.1	6.511	766.9	-53.1
7.010	791.3	-35.5	6.513	779.0	-48.1	7.008	767.7	-46.9
7.494	791.9	-29.5	7.000	779.7	-41.9	7.519	768.4	-41.3
7.989	792.6	-23.5	7.519	780.5	-36.1	8.008	769.2	-36.6
8.337 9.017	793.2	-10.0 -11.9	8 543	781.8	-263	8.303 9.019	709.9	-32.3 -28.3
9.636	794.6	-9.1	9.139	782.5	-21.5	9.506	771.3	-25.0
			9.497	783.0	-18.9	9.994	772.1	-22.0
			10.068	783.8	-15.2			
х	$T_1 = 0.2003_4$; $T/K =$	347.97	$x_1 =$	$= 0.4248_1$: T/K =	308.12	$x_1 =$	$= 0.4248_1$; T/K =	313.10
			4.780	807.5	-150.5	5.812	801.4	-108.2
5.098	745.6	-86.8	5.038	808.2	-132.9	6.012	801.7	-101.2
5.302	746.1	-80.1	5.326	808.8	-120.3	6.200	802.1	-95.0
5.535 6.025	740.5 777 7	- / 5.0	5.517	809.2 810 3	-112.0	0.373	802.0 803.1	-88.9 -82 7
6.609	748.4	-58.4	6.505	811.3	-78.1	6.803	803.5	-77.0
7.005	749.2	-53.4	6.515	811.4	-77.8	7.055	804.1	-70.1
7.508	750.1	-47.9	6.714	811.8	-71.6	7.208	804.3	-66.0
8.010	751.0	-43.0	7.035	812.4	-61.8	7.409	804.8	-60.7
8.501	751.7	-38.8	7.207	812.8	-56.6	7.611	805.2	-55.5
8.915 9 581	152.4 753 5	-35.0 -31.1	7.501	813.4 813.8	-47.2 -34.0	7.802 7.998	805.7 806.1	-50.7 -45.7
9.706	753.7	-30.3	8.024	814.4	-24.8	8.201	806.5	-40.4
10.014	754.2	-28.5	8.606	815.6	-14.4	8.597	807.3	-30.1
			8.802	816.0	-13.2	8.797	807.6	-25.4
			9.002	816.4	-12.2	9.024	808.1	-21.2
			9.529	817.3	-10.5	9.602	809.3	-15.5
			9.898	018.0	-9.0	10.055	010.1	-13.2
x	$r_1 = 0.4248_1; T/K =$	323.03	<i>x</i> ₁ =	$= 0.4248_1; T/K =$	333.02	$x_1 =$	$= 0.4248_1; T/K =$	347.93
6.842	786.9	-88.7	7.301	770.1	-87.9	7.801	744.8	-90.2
7 302	/8/.3 788 1	-84.4 -77.2	7.408 7.506	//0.5 770.6	-85.5 -83.3	7.908	/45.1 745 5	-88.1
1.504	/00.1	11.4	1.500	770.0	05.5	1.777	173.5	00.5

Table 2	(Continued)

P	ρ	$v^{\rm E}$	Р	ρ	$v^{\rm E}$	Р	ρ	$v^{\rm E}$
MPa	kg•m ⁻³	$\overline{\text{cm}^{3} \cdot \text{mol}^{-1}}$	MPa	kg•m ⁻³	$\overline{\text{cm}^3 \cdot \text{mol}^{-1}}$	MPa	kg•m ⁻³	$\overline{\text{cm}^3 \cdot \text{mol}^{-1}}$
<i>x</i> ₁ =	$= 0.4248_1; T/K =$	323.03	<i>x</i> ₁ =	= 0.4248 ₁ ; <i>T</i> /K =	= 333.02	x ₁ =	$= 0.4248_1; T/K =$: 347.93
7.530	788.6	-72.0	7.613	771.0	-81.0	8.130	745.9	-83.8
8.004	789.7	-62.0	7.806	771.4	-77.0	8.239	746.2	-81.8
8.302	790.4	-56.1	8.005	772.0	-73.1	8.408	746.8	-78.8
8.401	790.6	-54.2	8.209	772.6	-69.2	8.501	747.2	-77.2
8.500	790.8	-52.4	8.394	773.2	-65.9	8.600	747.4	-75.6
8.603	791.2	-50.5	8.802	774.1	-59.1	8.712	747.8	-73.7
8.710	791.4	-48.6	8.916	774.5	-57.2	8.801	748.2	-72.3
8.821	791.7	-46.7	9.000	774.7	-55.9	8.890	748.4	-70.9
9.000	792.1	-43.6	9.100	775.0	-54.4	9.033	748.8	-68.7
9.209	792.5	-40.2	9.205	775.3	-52.9	9.105	749.1	-67.7
9.309	792.8	-38.6	9.304	775.6	-51.4	9.244	749.4	-65.6
9.401	793.1	-37.2	9.410	775.8	-49.9	9.410	750.0	-63.3
9.502	793.3	-35.7	9.506	776.1	-48.6	9.501	750.2	-62.1
9.601	793.4	-34.2	9.607	776.4	-47.2	9.608	750.7	-60.7
9.728	793.7	-32.4	9.809	776.8	-44.6			
$x_1 =$	$= 0.6086_1; T/K =$	308.11	$x_1 =$	$= 0.6086_1; T/K =$	313.12	$x_1 =$	$= 0.6086_1; T/K =$	323.05
6.002	812.2	-133.2	6.801	802.8	-107.8	7.506	779.7	-101.1
6.221	813.0	-122.6	7.000	803.5	-100.0	7.703	780.7	-94.9
6.400	813.7	-114.3	7.203	804.4	-92.2	7.803	781.1	-91.9
6.606	814.5	-105.0	7.402	805.2	-84.8	7.910	781.7	-88.7
6.807	815.2	-96.1	7.602	806.0	-77.5	8.009	782.2	-85.8
7.019	815.9	-86.9	7.804	806.8	-70.1	8.208	783.1	-80.1
7.203	816.7	-78.9	8.010	807.7	-62.6	8.404	784.1	-74.8
7.401	817.4	-69.9	8.197	808.3	-55.7	8.607	785.0	-69.5
7.607	818.3	-59.9	8.400	809.1	-48.2	8.800	785.8	-64.6
7.804	818.9	-48.9	8.602	809.8	-40.7	9.004	786.7	-59.6
8.005	819.7	-34.6	8.812	810.5	-33.6	9.301	788.0	-52.8
8.209	820.4	-24.9	9.000	811.3	-28.7	9.501	788.9	-48.4
8.600	821.7	-18.4	9.213	812.0	-24.6	9.702	789.8	-44.3
8.810	822.4	-16.6	9.392	812.6	-22.1	9.805	790.2	-42.3
9.000	823.1	-15.3	9.600	813.3	-19.9			
9.101	823.3	-14.7	9.802	814.0	-18.2			
9.200	823.8	-14.3	10.001	814.6	-16.9			
r. =	$= 0.6086 \cdot T/K =$	333.02	r. =	= 0.6086. T/K =	3/17 9/	r. =	$= 0.79/3 \cdot T/K =$	308 11
8 226	- 0.0000], 1/K - 753 6	-74.5	0 800	- 0.0000[, 1/K - 716.0	-78.2	6.824	- 0.79431, 17K - 703 7	-122.1
8 305	754.3	-76.6	9.815	717.0	-78.2	7 001	795.6	-111.0
8.400	754.8	-78.9	9.813	718.1	-78.2	7.206	797 /	-09.4
8 504	755.5	-81.1	9.831	719.1	-78.1	7.200	799.2	-88.0
8 610	756.0	-83.4	9.840	719.7	-78.0	7.607	801.1	-74.9
8 701	756.6	-85.6	9.850	720.0	-77.9	7.810	803.0	-60.0
8.802	757.3	-88.1	9.861	720.0	-77.7	8.007	804.6	-41.9
8.900	757.9	-90.7	9.873	720.2	-77.5	8.197	806.2	-29.9
9.005	758.5	-93.1	9.885	720.2	-77.3	8.414	807.8	-24.0
9.103	759.0	-95.6	9 897	720.3	-77.1	8.618	809.6	-20.8
2.105	157.0	25.0	9.910	720.4	-76.8	8,796	810.8	-18.8
			9 949	720.8	-76.2	9.017	812.5	-17.0
			10.004	721.1	-75.2	9.203	813.9	-15.7
			10.052	721.5	-74.4	9 400	815.3	-14.6
			10.104	721.9	-73.6	9.607	816.6	-13.6
			10.152	722.2	-72.8	9.807	818.0	-12.8
						9.902	818.6	-12.5
	0.50.10	212.00		0.5010 577	222.04		0.50.10 577	222.05
x1 =	$= 0.7943_1; T/K =$	313.08	$x_1 =$	$= 0.7943_1; T/K =$	= 323.06	$x_1 = 0.720$	$= 0.7943_1; T/K =$	332.97
7.544	///.4	-102.0				9.739	080.8	-/0.1
7.601	//8.5	-97.2	0 704	745 2	02.0	9.804	689.2	- /4./
/.810	/80.8	-87.3	8.724	/45.3	-82.8	9.901	091.4	-/2.6
8.013	/83.0	-//./	8.802	/46.6	- /9.6	10.001	693.5	-/0.5
8.205 8.410	184.9	-08.0	8.905	747.9	-/0.4	10.101	095.0	-68.4
0.410	/ 80.8	-58./	9.005	149.2	-/3.3	10.201	097.8	-66.4
0.393	/ 88.4	-49.8	9.204	/31.0	-0/.4	10.302	099.9	-64.4
0.000	790.3	-40./	9.410	155.9	-01.5	10.404	/01./	-62.4
8.999 0.209	192.2	-55.9	9.606	/50.2	-50.2	10.50/	/03./	-60.5
9.208	/94.0	-28.8	9.792	/58.2	-51.5	10.000	703.4	-58.6
9.405	/95./	-25.2	10.001	/60.2	-40.6	10.808	/08.9	-55.0
9.619	/9/.5	-22.5	10.310	/63.1	-40.2	11.007	/12.0	-51.7
9.803	/99.0	-20.6				11.204	/15.0	-48.6
10.061	800.9	-18.5				11.404	/1/.8	-45.6
10.515	804.0	-15.7				11.607	720.5	-42.8
11.013	807.3	-13.5				11.805	722.9	-40.2
11.507	810.6	-11.9				12.004	725.3	-37.8
11.994	813.5	-10.6						
12.199	814.6	-10.2						
12.410	815.6	-9.7						
12.606	816.7	-9.3						

Table 2 (Continued

Р	ρ	$v^{\rm E}$	Р	ρ	$v^{\rm E}$	Р	ρ	$v^{\rm E}$
MPa	kg·m ⁻³	$\overline{\text{cm}^3 \cdot \text{mol}^{-1}}$	MPa	kg•m ⁻³	$\overline{\text{cm}^3 \cdot \text{mol}^{-1}}$	MPa	kg•m ⁻³	$\overline{\text{cm}^3 \cdot \text{mol}^{-1}}$
x1 =	= 0.79431: T/K =	= 347.95	$x_1 =$	$= 0.9492_0$; T/K =	= 308.12	$x_1 =$	= 0.9492 ₀ : <i>T</i> /K =	= 313.09
11.400	647.2	-63.0	7.302	699.6	-103.2	7.960	642.1	-82.6
11.604	653.3	-60.3	7.402	704.9	-96.6	8.001	648.3	-80.9
11.812	658.7	-57.6	7.605	713.8	-82.0	8.200	666.4	-71.2
12.007	663.0	-55.1	7.802	720.9	-65.3	8.400	677.7	-60.7
12.201	666.8	-52.8	8.002	728.0	-43.8	8.606	688.5	-49.7
12.502	672.6	-49.3	8.204	734.5	-29.0	8.803	697.0	-40.1
12.802	677.6	-46.1	8.404	740.3	-22.8	9.002	704.0	-32.5
13.202	684.0	-42.1	8.605	745.7	-19.3	9.201	710.9	-27.1
13.504	688.5	-39.5	8.802	750.6	-16.9	9.408	717.1	-23.1
13.802	692.8	-36.9	9.004	/55.4	-15.1	9.604	722.7	-20.3
14.109	090.9	-34.5	9.201	759.7	-13.7	9.800	728.1	-18.2
14.400	700.5	-32.4 -30.4	9.408	768.0	-11.6	10.003	737.5	-10.5
15,000	703.5	-28.6	9.805	700.0	-10.8	10.201	741 5	-13.8
15.000	709.6	-27.4	10.003	774.9	-10.0	10.405	744.7	-12.8
15.407	711.9	-26.4	10.202	778.0	-9.4	10.803	747.4	-11.8
15.610	714.0	-25.4	10.405	780.9	-8.9			
15.813	716.1	-24.4	10.617	783.7	-8.3			
16.004	717.9	-23.5	10.807	785.9	-7.9			
16.303	720.7	-22.3						
16.501	722.4	-21.5						
16.808	725.0	-20.3						
r1 =	$= 0.9492_{0} \cdot T/K =$	= 323.05	r1 =	$= 0.9492_{0} \cdot T/K =$	= 332 99	$\mathbf{r}_1 =$	$= 0.9492_{0} \cdot T/K =$	= 347 96
9.107	526.2	-58.2	10.561	502.4	-42.0	10.989	348.5	-263
9.400	575.3	-55.0	10.601	506.6	-41.8	11.505	382.4	-27.0
9.710	607.0	-48.9	10.709	517.4	-41.1	12.004	415.7	-27.1
10.015	628.2	-42.4	10.810	526.9	-40.4	12.507	448.4	-26.6
10.301	644.3	-36.8	10.910	536.2	-39.7	13.000	477.1	-25.4
10.600	658.2	-31.8	11.209	560.9	-37.2	13.503	503.0	-23.8
10.904	670.3	-27.5	11.503	580.0	-34.4	14.006	527.8	-22.3
11.211	681.1	-24.0	11.803	596.0	-31.4	14.511	550.1	-20.7
11.508	689.9	-21.3	12.102	611.4	-28.9	15.011	569.6	-19.1
11.807	698.3	-19.1	12.404	624.7	-26.5	15.495	586.6	-17.7
12.106	705.9	-17.2	12.705	635.9	-24.2	15.997	602.4	-16.3
12.404	/12.6	-15.6	13.010	645.6	-22.1	16.514	617.0	-15.0
12.705	719.2	-14.5	13.302	034.3 662.6	-20.4	17.014	629.5	-13.8
13 300	723.3	-13.2	13.005	671.7	-17.5	17.313	648.6	-12.7
13.608	736.7	-11.3	14 213	678.9	-16.2	17.900	040.0	11.0
13.907	742.0	-10.5	14.513	684.7	-15.0			
14.210	746.8	-9.8						
14.504	751.1	-9.2						
14.804	755.1	-8.6						
× -	$= 0.9715 \cdot T/V$ -	= 308 13	r =	$= 0.9715 \cdot T/K -$	= 313 12	r =	= 0.9715 + T/V =	= 323.05
7 456 x ₁ -	- 0.9/136; 1/K = 611 7	- 306.13 - 86.8	$x_1 = 8 124$	- 0.97136; 1/K = 526.2	- 513.12 	x ₁ =	- 0.7/136; 1/K = 303 0	- 323.05
7 502	636.2	-84 5	8 526	627 3	-497	9 031	381.9	-31.7
7 992	680.6	-41.7	9.002	662.5	-29.7	9 535	467.3	-34.2
8.522	706.8	-18.0	9.522	689.0	-19.3	10.046	540.0	-31.2
8.997	724.3	-13.0	10.021	708.1	-14.6	10.501	577.6	-25.4
9.508	739.8	-10.3	10.520	722.7	-11.8	11.011	612.9	-20.4
10.027	752.9	-8.5	10.993	734.9	-10.0	11.512	638.9	-16.8
10.521	763.7	-7.3	11.514	746.8	-8.5	12.028	660.4	-14.0
11.017	773.2	-6.3	12.038	757.3	-7.4	12.516	677.0	-12.0
11.500	781.6	-5.6	12.512	765.8	-6.6	13.014	691.5	-10.5
12.008	789.6	-4.9	13.003	773.6	-5.8	13.558	705.3	-9.1
12.520	797.2	-4.4	13.500	781.1	-5.2	14.003	715.4	-8.2
13.012	803.8	-3.9	13.998	788.2	-4.7	14.516	725.9	-7.3
15.520	810.4	-3.5	14.495	/94.8	-4.2	15.024	135.4	-6.6
14.014	010.4 822 1	-3.2	15.008	001.1	-3.8	13.300	/43.0	-0.0
14.320	022.1 827 3	-2.9 -2.6						
12.000	041.0	4.0						

certainty of density data in the liquid phase is estimated to be within \pm 0.05 % with a minimum value of \pm 0.2 kg·m⁻³, due to the uncertainties of the mechanical parameters used in the FPMC model. Global temperature uncertainties are estimated to be about \pm 0.02 K, which includes the temperature uncertainty of the bath regulation. Global uncertainties of pressure measurements after calibration are (\pm 0.00015, \pm 0.001, and \pm 0.002) MPa, respectively, to the sensor's ranges: (0.2, 5, and 40) MPa. Uncertainties of mixture compositions are within \pm 2·10⁻⁴ in mole fraction.

3. Experimental Results and Modeling

Table 2 presents the experimental liquid density data sets for six compositions of the carbon dioxide + 2-propanol binary system at five temperatures. Our experimental liquid density data are compared with those of Yaginuma et al.,³ who used the variable volume cell to measure the density for different compositions, and presented in Figure 2. Deviations, calculated using eqs 6 and 7, are presented in Table 3. As can be seen, they are in relative agreement with the selected literature data.



Figure 2. $P\rho T$ data of the carbon dioxide (1) + 2-propanol (2) binary system. (A) Experimental data of Yaginuma et al.³ at 313.15 K: \blacklozenge , $z_1 = 0.20$; \blacksquare , $z_1 = 0.40$; \blacktriangle , $z_1 = 0.60$. Our work at 313.10 K: \bigcirc , $z_1 = 0.2003$; +, $z_1 = 0.4248$; -, $z_1 = 0.6086$. (B) Experimental data of Yaginuma et al.³ at 313.15 K: \blacklozenge , $z_1 = 0.80$; \blacktriangle , $z_1 = 0.97$. Our work at 313.10 K: \square , $z_1 = 0.7943$; \times , $z_1 = 0.9715$.

Table 3. Density Deviations between Our Data and Those from Yaginuma et al. $\!\!^3$

our work	Yaginuma et al.3	deviations (e	eqs 6 and 7)
T/K = 313.10	T/K = 313.15	absolute	relative
<i>x</i> ₁	<i>x</i> ₁	kg•m ⁻³	%
0.2003	0.20	-0.41	0.05
0.6086	0.60	-0.18	0.02
0.7943	0.80	-3.98	0.51
0.9715	0.97	-11.73	1.75

In addition to simultaneous measurement of density, the vibrating tube densimeter allows estimation of bubble points as shown by Bouchot and Richon.⁵ Figure 3 shows how these points are determined. Table 4 presents the results. To evaluate the accuracy of our experimental method, a comparison with literature data was done.

Bamberger and Maurer¹⁰ have previously studied this system at three temperatures, (293, 313, and 333) K. They developed

a model to correlate their experimental data. They considered a symmetric approach to calculate PTxy properties involving the Peng-Robinson equation of state (PR EoS) (eq 1).

$$P = \frac{RT}{v - b} - \frac{a}{v(v + b) + b(v - b)}$$
(1)

where *P* is the pressure (Pa); *T* represents the temperature (K); *R* stands for the molar gas constant (8.314 J·mol⁻¹·K⁻¹); *a* is the attractive parameter of the EoS; *b* is the molar covolume; and *v* is the molar volume of the mixture (m³·mol⁻¹). The pure component properties are indicated in Table 1.

The Panagiotopoulos and Reid¹¹ mixing rules are used to extend the PR EoS to mixtures.

$$b = \sum_{i} x_{i} b_{i} \tag{2}$$



Figure 3. Graphical determination of bubble points on the pressure-period diagram.

$$a = \sum_{i} \sum_{j} x_{i} x_{j} a_{ij} \tag{3}$$

For a binary system, a_{ij} is determined using a specific function involving the binary interaction parameter and attractive parameter *a* for components *i* and *j*

$$a_{ij} = (1 - k_{ij} - (k_{ij} - k_{ji})x_i)\sqrt{a_i a_j}$$
(4)

The attractive parameter contain two terms ($a = \alpha(T,T_C)a_C$). α is called the alpha function which takes into account temperature dependence of *a*. In their paper, Bamberger and Maurer used the following alpha function (Mehlem et al.¹³)

$$\ln(\alpha_{i}(T,T_{Ci})) = m \left[1 - \frac{T}{T_{Ci}}\right] + n \left[1 - \sqrt{\frac{T}{T_{Ci}}}\right]^{2}$$
(5)

where x_i is the molar fraction of the component *i* (*i* = 1 or 2, CO₂ and 2-propanol, respectively), and T_{Ci} and P_{Ci} are, respectively, the critical temperature and pressure of component *i*. The parameters *m*, *n*, k_{12} , and k_{21} , determined by Bamberger and Maurer,¹⁰ are given in Table 5.

Deviations (see Table 4) between calculated and experimental data are expressed by expressions 6 and 7.

relative deviation: dev % =
$$\frac{100}{N} \sum_{N} \left(\frac{|U_{\text{exptl}} - U_{\text{calcd}}|}{U_{\text{calcd}}} \right)$$
 (6)

absolute deviation:
$$dev = \frac{100}{N} \sum_{N} (U_{exptl} - U_{calcd})$$
 (7)

4. Comparison with Literature Data and Discussion

Isothermal $P\rho T$ and Excess Volume Data of the Mixture. To compare the capability of the previous model to calculate volumetric properties, we have considered the excess volume for all the mixtures (see Table 2). They are calculated using eq 8

$$v^{\rm E} = v - (x_1 v_1 + x_2 v_2) \tag{8}$$

Table 4. Comparison between the Bubble Point Experimental Data Determined for the CO_2 (1) + 2-Propanol (2) Binary System and the Calculated Value Obtained with the Model Developed by Bamberger and Maurer

calcd with Ban	n the model deve nberger and Mau	experin	nental work	
		Pcalcd	Pexptl	deviation
x_1	y1calcd	MPa	MPa	%
	T	K = 313.10		
0.1390	0.9904	2.26	2.28	0.73
0.2003	0.9918	3.13	3.64	14.13
0.4248	0.9918	5.56	5.85	4.90
0.6086	0.9902	6.68	6.78	1.43
0.7943	0.9890	7.19	7.54	4.68
0.9492	0.9876	7.85	7.96	1.35
0.9715	0.9865	8.08	8.10	0.30
	Т	K = 308.10		
0.1390	0.9924	2.15	1.76	-22.17
0.2003	0.9935	2.96	2.75	-7.64
0.4248	0.9936	5.19	4.78	-8.64
0.6086	0.9927	6.16	5.95	-3.46
0.7943	0.9921	6.56	6.82	3.75
0.9492	0.9922	7.18	7.27	1.23
0.9715	0.9928	7.41	7.45	0.54
	Т	K = 323.07		
0.1390	0.9852	2.49	2.66	6.51
0.2003	0.9873	3.45	4.05	14.77
0.4248	0.9870	6.3	6.81	7.44
0.6086	0.9835	7.77	7.87	1.33
0.7943	0.9791	8.5	8.72	2.50
	T	K = 333.00		
0.1390	0.9779	2.71	2.82	4.05
0.2003	0.9810	3.77	4.21	10.45
0.4248	0.9805	7.03	7.23	2.78
0.6086	0.9736	8.85	8.23	-7.58
0.7943	0.9613	9.87	9.72	-1.52
	T	K = 348.00		
0.1390	0.9619	3.03	3.32	8.76
0.2003	0.9674	4.23	5.10	17.00
0.4248	0.9665	8.07	7.72	-4.56
0.6086	0.9530	10.43	10.00	-4.32
0.7943	0.9148	11.87	11.35	-4.61

where v_1 and v_2 are the experimental pure component molar volumes calculated with the PR EoS; x_1 and x_2 represent the

Table 5. Component Parameters from Bamberger and Maurer¹³

	alpha f paramete	unction ers (eq 5)	Panagiotopou mixing ru interaction	llos and Reid les binary parameters
compd	m	n	k ₁₂	k ₂₁
carbon dioxide 2-propanol	0.6877 1.1979	0.3813 0.8456	0.1467	0.1005

mole fractions of carbon dioxide and of 2-propanol, respectively; and v is the molar volume of the mixture.

Figure 4 shows the experimental excess volume data compared to the excess volumes calculated using the Peng– Robinson equation of state and some literature data. Our experimental data seem to be in good agreement with the literature data and the calculated data except for the composition of 0.9492 where the mixture is near its critical temperature.

According to Figure 4, it can be seen that excess molar volume is negative particularly for the high concentration of CO_2 . It is probably due to a packing effect between the two molecules. Moreover, the PR EoS gives a good representation of excess molar volume. Observed deviations are within (\pm 2.1) cm³·mol⁻¹. Figure 5 shows the experimental excess volume data compared to the excess volumes calculated using the Peng–



Figure 4. Excess molar volumes of the carbon dioxide (1) + 2-propanol (2) binary system as a function of composition at 313 K and 8 MPa. \triangle , Zuniga-Moreno et al.;⁴ \Box , Yaginuma et al.;³ \blacklozenge , this work. Solid line, calculated with the model developed by Bamberger and Maurer.



Figure 5. Excess molar volumes of the carbon dioxide (1) + 2-propanol (2) binary system as a function of CO₂ composition at 8 MPa and five temperatures. This work at: \times , 308.10 K; \Box , 313.10 K; \diamond , 323.06 K; Δ , 333.06 K; \bigcirc , 348.00 K. Solid line, calculated with the model developed by Bamberger and Maurer.



Figure 6. Vapor–liquid equilibrium data for temperatures around 313 K concerning the binary system CO₂ (1) + 2-propanol (2). ×, Bamberger and Maurer data at 313.2 K; \Box , Yaginuma et al. at 313.15 K; \bigcirc , Lazzaroni et al.¹⁴ at 313 K; \triangle , this work at 313.10 K. Solid line: bubble point curve calculated with the PR EoS at 313.11 K.

Robinson equation of state. Our experimental data seem to be in good agreement with data calculated using the PR EoS except for at the temperature of 308.10 K where the model results are slightly out of the deviation's range.

Vapor-Liquid Equilibrium (VLE). The experimental VLE data and their deviations are given in Table 4, and some of them are shown in Figure 6 and are compared with selected literature data. To predict our VLE data, we have used the PR EoS and the Panagiotopoulos and Reid mixing rules. According to Table 4, we can see that our experimental data are in relatively good agreement with predicted VLE data by the PR EoS. The deviations are probably due to the difficulty in determining very accurately the break point and also due to the fact that Bamberger and Maurer gave temperature-independent binary interaction parameters. Consequently, we can consider that the presented technique is convenient to get accurate PVT data and satisfactory to estimate bubble pressures. In fact, bubble pressure measurements are really more accurate using the variable volume cell technique (Fontalba et al.¹⁵) or static analytic method (Laugier and Richon¹⁶).

5. Conclusion

A vibrating tube densimeter, taking advantage of a forced path mechanical calibration model, was used for generating new volumetric properties, and the experimental data were generated in a large range of carbon dioxide compositions, particularly for new compositions close to one in carbon dioxide (i.e., 0.15, 0.20, 0.42, 0.61, 0.80, 0.95, and 0.97), and at temperatures between (308.15 and 348.15) K. The reliability of the data was finally tested with the results of a model based on the Melhem et al. modification of the Peng–Robinson equation of state with the Panagiotopoulos and Reid mixing rules as well as with some selected data from the literature. The determination of the bubble point from density data shows satisfactory agreement with VLE data from the literature.

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